

KEY

No Calculator

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Hour: _____

Top 20 ACT Prep Version 5

1. Given $f(x) = -4x^2 - 2x - 3$, find $f(-2)$

$$\begin{aligned} [110] \quad f(-2) &= -4(-2)^2 - 2(-2) - 3 \\ &= -4(4) + 4 - 3 \\ &= -16 + 4 - 3 \end{aligned}$$

$$\boxed{f(-2) = -15}$$

2. Simplify $(5a - 9n)^2$

$$\begin{aligned} (5a - 9n)(5a - 9n) \\ 25a^2 - 45an + 81n^2 - 45an \\ \boxed{25a^2 - 90an + 81n^2} \end{aligned}$$

3. Solve $21x^2 - 15x - 6 = 0$

$$3(7x^2 - 5x - 2) = 0 \quad 7x + 2 = 0$$

$$7x^2 - 7x + 2x - 2 = 0 \quad 7x = -2$$

$$7x(x-1) + 2(x-1) = 0 \quad \boxed{x = -\frac{2}{7}}$$

$$(7x+2)(x-1) = 0 \quad x-1 = 0$$

$$\boxed{x = 1}$$

4. Find the distance between $(0, -2)$ & $(5, 7)$

$$\begin{aligned} [217] \quad d &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(5 - 0)^2 + (7 - (-2))^2} \\ &= \sqrt{5^2 + 9^2} = \sqrt{25 + 81} \end{aligned}$$

$$\boxed{d = \sqrt{106}}$$

5. Simplify $\frac{4}{9} \cdot \frac{7}{8}$

$$\frac{4}{9} \cdot \frac{7}{8} = \frac{7}{18}$$

6. Simplify $\frac{-2 \pm \sqrt{8}}{12}$

$$\begin{aligned} \frac{-2 \pm \sqrt{8}}{12} &= \frac{-2 \pm 2\sqrt{2}}{12} \\ \frac{-1 \pm \sqrt{2}}{6} &= \frac{-1 \pm \sqrt{2}}{6} \text{ or } \frac{-1 \pm \sqrt{2}}{6} \end{aligned}$$

7. Simplify $\frac{27x^5y^2}{9x^2z^3}$

$$\frac{3x^3y}{z}$$

8. Simplify $\frac{3}{4} \cdot \frac{9}{5}$

$$\frac{3}{4} \cdot \frac{9}{5} = \frac{27}{20}$$

9. Multiply $(x^2 + 2)(x - 5)$

$$\boxed{x^3 - 5x^2 + 2x - 10}$$

10. Simplify $(2a^4b^3)^3 \cdot 3(a^2b^3)$

$$\begin{aligned} (2^3)a^{12}b^9 \cdot 3a^2b^3 &= 8a^{12}b^9 \cdot 3a^2b^3 \\ &\rightarrow \boxed{24a^{14}b^{12}} \end{aligned}$$

11. Solve $(x - 6)^2 = 14$

$$\begin{aligned} \sqrt{(x-6)^2} &= \sqrt{14} \\ x-6 &= \pm\sqrt{14} \\ \boxed{x = 6 \pm \sqrt{14}} \end{aligned}$$

12. Simplify $2\frac{3}{4} - \frac{2}{5}$

$$\begin{aligned} \frac{4}{4} \cdot \frac{11}{4} \cdot \frac{3}{4} - \frac{2}{5} &= \frac{55}{20} - \frac{8}{20} \\ \frac{11}{4} - \frac{2}{5} &= \frac{11(5)}{4(5)} - \frac{2(4)}{5(4)} \rightarrow \frac{55}{20} - \frac{8}{20} = \frac{47}{20} \end{aligned}$$

13. Clear fractions, solve $\frac{4}{9}a + 2 = \frac{1}{4}$

$$\begin{aligned} \frac{4}{9}a + \frac{8}{4} &= \frac{1}{4} \\ \frac{4}{9}a &= \frac{1}{4} - \frac{8}{4} \\ \frac{4}{9}a &= \frac{-7}{4} \\ a &= \frac{-63}{16} \end{aligned}$$

14. Find 3 points on $f(x) = x^2 + 3x - 7$

* Many possible pts.
ex) $f(0) = (0)^2 + 3(0) - 7 = -7$

$$f(1) = (1)^2 + 3(1) - 7 = -3$$

$$f(-1) = (-1)^2 + 3(-1) - 7 = -9$$

X	Y
0	-7
1	-3
-1	-9

15. Simplify $\frac{x^2 - 7x - 44}{x^2 - 121}$

$$\frac{(x-11)(x+4)}{(x+11)(x-11)} = \frac{x+4}{x+11}$$

16. Find the midpoint given $(0, 5)$ & $(10, -3)$

$$\frac{\Delta x}{2} = \frac{10 - 0}{2} = 5 \quad \Delta x + x_1 = 5 + 0 = 5$$

$$\frac{\Delta y}{2} = \frac{-3 - 5}{2} = \frac{-8}{2} = -4 \quad \Delta y + y_1 = -4 + 5 = 1$$

$$\boxed{\text{midpoint: } (5, 1)}$$

17. Write an equation using $(12, 7)$ & $(-9, -3)$

$$[210] \quad m = \frac{\Delta y}{\Delta x} = \frac{-3 - 7}{-9 - 12} = \frac{-10}{-21} = \frac{10}{21}$$

$$y = mx + b$$

$$7 = \frac{10}{21}(12) + b$$

$$b = \frac{27}{21}$$

$$\boxed{y = \frac{10}{21}x + \frac{27}{21}}$$

$$\boxed{y + 3 = \frac{10}{21}(x + 9)}$$

$$\boxed{y - 7 = \frac{10}{21}(x - 12)}$$

18. Simplify (PEMDAS) $-2(x - 1)^2 + 6$

$$-2(x-1)(x-1) + 6 \rightarrow -2x^2 + 4x - 2 + 6$$

$$-2(x^2 - 2x + 1) + 6 \rightarrow \boxed{-2x^2 + 4x + 4}$$

19. Solve $V = \pi r^2 h$ for r

$$\sqrt{r^2} = \sqrt{\frac{V}{\pi h}} \rightarrow \boxed{r = \pm \sqrt{\frac{V}{\pi h}}}$$

20. Solve. Show 3+ steps of work

$$-(6x + 4) + 2(x - 8) = 11x + 4$$

$$-6x - 4 + 2x - 16 = 11x + 4$$

$$-4x - 20 = 11x + 4$$

$$-24 = 15x$$

$$x = \frac{-24}{15} \rightarrow \boxed{\frac{-8}{5} = x}$$

